

# EXPERIMENTAL COMPARISON OF WIDE BASELINE CORRESPONDENCE ALGORITHMS FOR MULTI CAMERA CALIBRATION

Ferid Bajramovic, Michael Koch, Joachim Denzler

*Chair for Computer Vision, Friedrich Schiller University of Jena, Ernst-Abbe-Platz 2, 07743 Jena, Germany*  
{bajramov,koch,denzler}@informatik.uni-jena.de

Keywords: correspondence, calibration, structure-from-motion, uncertainty.

Abstract: The quality of point correspondences is crucial for the successful application of multi camera self-calibration procedures. There are several interest point detectors, local descriptors and matching algorithms, which can be combined almost arbitrarily. In this paper, we compare the point correspondences produced by several such combinations. In contrast to previous comparisons, we evaluate the correspondences based on the accuracy of relative pose estimation and multi camera calibration.

## 1 Introduction

Calibration is an important prerequisite for many applications of multi camera systems. The most convenient, but also the most challenging class of calibration methods uses only images from the cameras as input—without any scene knowledge or user interaction (Martinec and Pajdla, 2007; Vergés-Llahí et al., 2008; Bajramovic and Denzler, 2008). The success of such methods crucially depends on the point correspondences which are extracted from the images in the first step.

Correspondence extraction typically consists of three steps: detection of points (or regions) of interest, computation of a local descriptor for each point, and matching of the descriptors. In this paper, we experimentally compare several alternative algorithms for all three steps. Unlike other comparisons (Mikolajczyk et al., 2005; Mikolajczyk and Schmid, 2005), we evaluate, how well the various correspondence methods are suited for relative pose estimation and multi camera calibration.

The paper is structured as follows. In Section 2, we briefly describe the detectors, descriptors and matching algorithms. Section 3 continues with the geometry estimation. In section 4, we present our experimental comparison. Conclusions are given in section 5.

## 2 Correspondences

In this section, we describe the methods which extract pairwise point correspondences from images. A point correspondence is a pair of 2D image points in two different images which represent the same 3D scene point. There is a general scheme for extracting point correspondences. The first step detects interest points in each image. They should be invariant against different 3D world transformations and changes in illumination, such that they can be found in different views of the same scene. Afterwards, a descriptor is calculated for every interest point which usually stores information of the surrounding area of the 2D image point. The last step consists of matching the descriptors in order to establish correspondences between 2D points in different images.

### 2.1 Detectors

The detection of interest points is a wide-spread field. In recent years, many different kinds of detectors have been developed. The most important attribute is the afore mentioned invariance. Most of the detectors are invariant against rotation, translation and scale. We base our selection on the work of Mikolajczyk et al. (Mikolajczyk et al., 2005; Mikolajczyk and Schmid, 2005).

### 2.1.1 Harris-Laplace

The Harris-Laplace (HarLap) detector (Mikolajczyk and Schmid, 2002) is based on the Harris-Stephens corner detector (Harris and Stephens, 1988). In addition, it uses a Gaussian scale space to achieve scale invariance. Hence, the second moment matrix becomes:

$$S = \sigma_D^2 \cdot g(\sigma_I) * \begin{pmatrix} I_x^2(x, \sigma_D) & I_x I_y(x, \sigma_D) \\ I_x I_y(x, \sigma_D) & I_y^2(x, \sigma_D) \end{pmatrix}. \quad (1)$$

The variable  $\sigma_I$  indicates the scale space kernel and  $\sigma_D$  designates the Gaussian smoothing kernel of the Gaussian function  $g$ .  $I_x(x, \sigma_D)$  and  $I_y(x, \sigma_D)$  define the smoothed derivatives in the corresponding image directions. The Harris-Stephens corner detector is applied to different scales and a specific scale is chosen by an iterative algorithm (Lindeberg, 1998). Afterwards, the interest points are selected according to the “cornerness”  $c = \det(S) - \alpha \cdot \text{trace}^2(S)$ . The constant  $\alpha$  is usually set to 0.04.

### 2.1.2 Hessian-Laplace

For the Hessian-Laplace (HesLap) detector (Mikolajczyk et al., 2005) the second moment matrix is replaced by the Hessian. Points which are local extrema of both, the determinant and the trace of the Hessian, are selected as interest points.

### 2.1.3 Affine Regions

The affine region detectors (HarAff, HesAff) extend the Harris-Laplace and Hessian-Laplace detectors by an iterative algorithm (Mikolajczyk and Schmid, 2002) which computes the second-moment matrix or the Hessian matrix, respectively, which transforms the anisotropic region into a normalized region.

### 2.1.4 Difference of Gaussian

The difference of Gaussian (DOG) detector described by Lowe (Lowe, 2004) uses a difference of Gaussian scale space to detect interest points. The main aspect is the scale invariance of the keypoints. The problem of the strong response to edges is solved by using the Harris-Stephens detector (Harris and Stephens, 1988) to suppress unstable keypoints along edges.

### 2.1.5 Intensity Based Regions

The intensity based regions (IBR) detector (Tuytelaars and van Gool, 2000) uses only the image intensity information. First, local extrema in the image are detected using non-maximum suppression. Afterwards, the developing of the intensity values on rays

with different angles starting from the extremum is analyzed. On each ray, one local extremum of a special intensity function is computed. Those are used to fit an ellipse to get a region which is invariant against affine transformations and additive illumination.

## 2.2 Descriptors

Next, we will introduce the descriptors used in our comparison. As mentioned before, they attempt to describe the interest points as invariantly as possible based on the image information.

### 2.2.1 SIFT

The scale invariant feature transform (SIFT) descriptor was first described by Lowe (Lowe, 2004). It generates a special gradient histogram as a vector of 128 entries from the area around the interest point.

### 2.2.2 Gradient Location and Orientation Histogram

Gradient Location and Orientation Histogram (GLOH) (Mikolajczyk and Schmid, 2005) is an extension of SIFT. It computes the SIFT descriptor on a log-polar location grid with different radial and angular directions in a total of 17 parameters for location. Gradient orientations are quantized to 16 values. The dimension of the resulting vector is reduced from 272 to 128 by principal component analysis (PCA).

### 2.2.3 Steerable Filters

Steerable filters (JLA) use derivatives computed by convolution with Gaussian derivatives using  $\sigma = 6.7$  (Freeman and Adelson, 1991) for an image patch. The derivatives are calculated up to fourth order and the resulting descriptor has dimension 14.

### 2.2.4 Moments

Moment invariants (MOM) (van Gool et al., 1996) describe the intensity and shape distribution information surrounding a keypoint (image region  $\Omega$ ). They are defined by  $M_{pq}^{ad} = \int \int_{\Omega} u^p v^q (I_d(u, v))^a dudv$  with order  $p + q$  and degree  $a$  using image gradients  $I_d$  in  $x$  and  $y$  direction ( $d \in \{x, y\}$ ). The invariant moments are computed up to second order and second degree. Hence, the resulting descriptor has dimension 20.

## 2.3 Matching

After computing the sets of descriptors  $\mathcal{A}$  and  $\mathcal{B}$  for all interest points in two images, we compute correspondences as a subset of  $C = \mathcal{A} \times \mathcal{B}$ . We limit the number of correspondences to 100 in each image pair.

### 2.3.1 Exhaustive Search

The exhaustive search (ES) matching builds a matrix  $D$  which consists of the distance measures between the descriptors for each element of  $C$  with

$$D = (d_{ij}), d_{ij} = \text{dist}(a_i, b_j), a_i \in \mathcal{A} \text{ and } b_j \in \mathcal{B}. \quad (2)$$

Normally, the distance measure  $\text{dist}$  is Euclidean. Point correspondences are selected by choosing the  $k$  interest points with minimum descriptor distances incrementally according to the uniqueness constraint.

### 2.3.2 Nearest Neighbor Matching

In the first step of nearest neighbor (NN) matching, a set of correspondence candidates is constructed. Each element of the descriptor set  $\mathcal{B}$  is assigned to the nearest neighbor in  $\mathcal{A}$ . The second step is identical to exhaustive search. From the initial set, the best  $k$  correspondences are selected incrementally enforcing the uniqueness constraint. The main difference to exhaustive search can be interpreted as considering only part of the matrix  $D$  for the final selection.

### 2.3.3 Two Nearest Neighbor Matching

Two nearest neighbor (2NN) is an extension of nearest neighbor matching described by (Lowe, 2004) aimed at removing ambiguous matchings. When matching a given descriptor in  $\mathcal{B}$  to its nearest neighbor in  $\mathcal{A}$ , we also compute the distance to the second nearest neighbor. A candidate match is only established if the ratio of the two distances is below a certain threshold (typically 0.8).

### 2.3.4 K-Hungarian Matching

The Hungarian (Hun) method is used for “minimum weight” bipartite graph matching. It is also applicable for matching point correspondences as shown by Keyzers et al. (Keyzers et al., 2004). In this context, the interest points in two images become the vertices of the complete bipartite graph. The edge weights are given by the distance between the descriptors of the two points. The Hungarian matching computes the optimal solution in the sense of least summed descriptor distance of all point correspondences.

The problem of this method are the high computational costs of  $O(m^2n^2)$  with  $m = |\mathcal{A}|$  and  $n = |\mathcal{B}|$ . Hence, we propose the following approximation which consists of reducing the number of interest points and thus vertices in the bipartite graph. We first calculate  $l < \min(m, n)$  initial correspondences  $\hat{C} \subseteq C$  using another method that needs less time than the Hungarian method. In the experiments, we use exhaustive search.

The set  $\hat{C}$  induces a subset of  $l$  interest points in each image:  $\hat{\mathcal{A}} \subseteq \mathcal{A}$  and  $\hat{\mathcal{B}} \subseteq \mathcal{B}$ . The subset  $\hat{\mathcal{A}}_k$  of interest points in the first image used for the Hungarian method is computed incrementally as follows: begin with  $\hat{\mathcal{A}}$  and for each point  $p \in \hat{\mathcal{B}}$ , add the  $k$  nearest neighbors within  $\mathcal{A} \setminus \hat{\mathcal{A}}_k$ . The subset  $\hat{\mathcal{B}}_k$  is defined accordingly. The number of vertices in the resulting complete bipartite graph is at most  $2l(k+1)$ . Applying the Hungarian method to it produces at most  $l(k+1)$  correspondences. The exact number of correspondences can vary greatly.

The total runtime of our approximate Hungarian matching consists of the initial extraction of  $l$  correspondences, building the reduced bipartite graph and applying the Hungarian method. The complexity of the last step will typically dominate the whole algorithm and is  $O((l \cdot (k+1))^4)$ .

## 3 Calibration

Given a set of cameras with known intrinsic parameters, we want to estimate the extrinsic parameters up to a similarity transformation. We use our procedure described in (Bajramovic and Denzler, 2008). We first estimate pairwise relative poses, which are subsequently composed to absolute poses. We will briefly describe both steps in this section. For details, the reader is referred to the afore mentioned paper.

### 3.1 Relative Pose Estimation

We use the five point algorithm (Stewénius et al., 2006; Brückner et al., 2008) to estimate relative poses (up to scale) between camera pairs with sufficiently many point correspondences and known intrinsic parameters. As the point correspondences must be expected to contain false matches (outliers), we embed the five point algorithm into a robust sampling algorithm (Bajramovic and Denzler, 2008; Engels and Nistér, 2005) similar to the RANSAC (Fischler and Bolles, 1981) variant MLESAC (Torr and Zisserman, 2000). There are two differences to RANSAC:

1. Instead of computing a support set, a probability density function  $p(\mathbf{R}, \mathbf{t} | \mathcal{D})$  is evaluated for

each hypothesis  $(\mathbf{R}, \mathbf{t})$  with regard to all correspondences  $\mathcal{D}$ . I.e. the sampling process approximates  $\operatorname{argmax}_{\mathbf{R}, \mathbf{t}} p(\mathbf{R}, \mathbf{t} | \mathcal{D})$ . Outliers are incorporated by using the Blake-Zisserman distribution.

2. A discrete approximation to  $p(\mathbf{t} | \mathcal{D})$  is built during the iteration. Its entropy is used as an uncertainty measure  $w(\hat{\mathbf{R}}, \hat{\mathbf{t}})$  for the resulting relative pose estimate  $(\hat{\mathbf{R}}, \hat{\mathbf{t}})$ .

### 3.2 Multi Camera Calibration

We (Bajramovic and Denzler, 2008) compose relative poses to absolute ones by first estimating the unknown scale factors in the estimated relative poses (up to a common unknown scale factor) and then concatenating the later. The procedure can be formalized by using the camera dependency graph which consists of a vertex for each camera and an edge for each known relative pose. We use triangulation to estimate the scale factors and hence have to work on triangles in the graph. As triangulation only eliminates two out of three unknown scale factors, we arbitrarily choose one of the scale factors in the first triangle and subsequently propagate scale factors from triangle to triangle. Moving from triangle to triangle can be expressed as traversing an auxiliary graph which represents the triangles as vertices.

As only a subset of relative poses is actually required for that process, the traversal order implies a selection of relative poses. We use the uncertainty measures computed during relative pose estimation to guide that selection. The main idea consists of interpreting the uncertainties as edge weights in the camera dependency graph and calibrating along a set of shortest triangle paths. Algorithmically, such paths are computed by applying Dijkstra to an extension of the triangle graph. Using shortest triangle paths is equivalent to selecting the subset of relative poses with minimum total uncertainty.

## 4 Experiments

We use two different experimental setups. The first one consists of two AVT Marlin monochrome cameras and six AVT Pike color cameras observing a scene, as depicted in Figure 1. We estimate the intrinsic camera parameters using Zhang’s (Zhang, 2000) calibration pattern based method. To be able to evaluate our calibration results, we use Zhang’s method also to compute a “ground truth” for the extrinsic calibration. Note that this “ground truth” is *not* free of errors, but still provides a reasonable comparison. For the second experiment, we use a robot arm to move a

Sony DFW-VL500 camera to 15 different poses. The arm provides us with reliable ground truth poses.

We use the detectors and descriptors implementation of Mikolajczyk et al. (Mikolajczyk et al., 2005; Mikolajczyk and Schmid, 2005) except for IBR. For the DOG-SIFT combination, we alternatively also use the SIFT++ implementation (Vedaldi, 2007).

### 4.1 Error Measures

In order to measure the accuracy of relative pose estimates, we compare the estimated translation vector to the ground truth. As the scale *and* sign are undetermined, we use the angle in degree between the two vectors ignoring direction, i.e. the error is at most  $90^\circ$ . Each experiment is repeated 10 times, as the results depend on random sampling. The accuracy of relative pose estimates is evaluated using all images pairs and all repetitions.

In order to evaluate a multi camera calibration, it first has to be registered with the ground truth to compensate for the undetermined similarity transformation. We use a randomized least median of squares estimator based on a nonlinear registration algorithm with linear initialization. We take the median distance between calibrated and ground truth camera positions as error measure for the multi camera calibration. The scale of the error measure is determined by the scale of the ground truth, which is normalized such that the first two cameras have distance 100.

### 4.2 Results

First, we analyze the matching algorithms and then compare detectors and descriptors using only the best matching method. Figures 2 and 3 show the errors on the relative pose estimates and the multi camera calibration. The results are aggregated over all detectors and descriptors in a boxplot (Tukey, 1977). A boxplot contains a box depicting the 0.25 and 0.75 quantiles. The line in the box is the median. The bars indicate the remaining spread. Crosses are outliers.

Two nearest neighbor (2NN) gives the best results, closely followed by nearest neighbor (NN). The high error outliers of 2NN can be explained by the fact that it produces no correspondences when applied to the IBR detector. Exhaustive search (ES) shows similar performance in the multi camera experiment, but is considerably worse on the robot arm data. The results for K-Hungarian (Hun) matching are quite poor.

Figures 4 and 5 show the relative pose errors and the multi camera calibration errors, respectively, using 2NN matching for all detector and descriptor combinations – except for IBR, which uses NN. The



Figure 1: Experimental setups. Left: the multi camera system used in the first experiment observing the pattern for the Zhang calibration, middle: the according scene (image from the sixth camera), right: the scene used in the robot arm experiment.

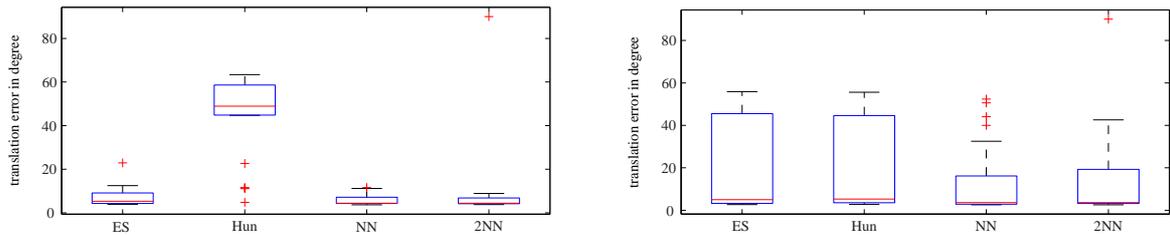


Figure 2: Relative poses: median of translation errors in degrees as a boxplot (Tukey, 1977), which is described briefly in the text. Left: multi camera system, right: robot arm.

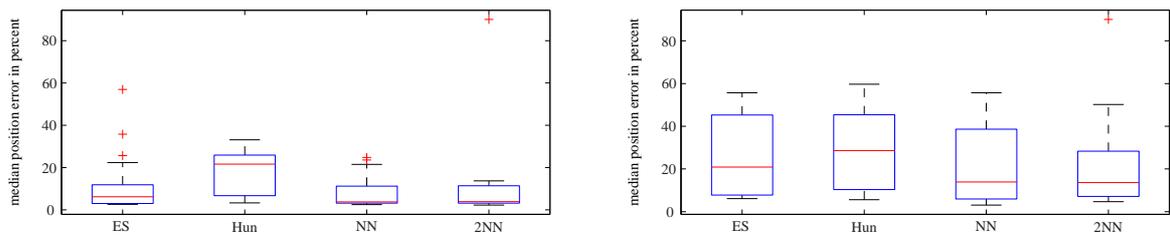


Figure 3: Multi camera calibration: median of median camera position errors in percent as a boxplot (Tukey, 1977), which is described briefly in the text. Left: multi camera system, right: robot arm.

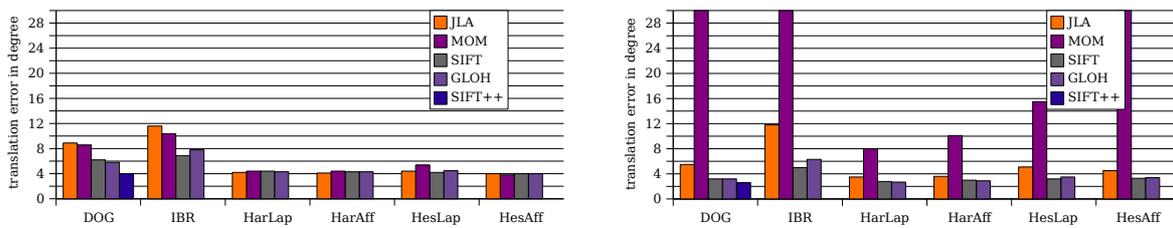


Figure 4: Relative poses: median of translation errors in degrees (truncated at 30) for all detectors and descriptors using nearest neighbor matching. Left: multi camera system, right: robot arm.

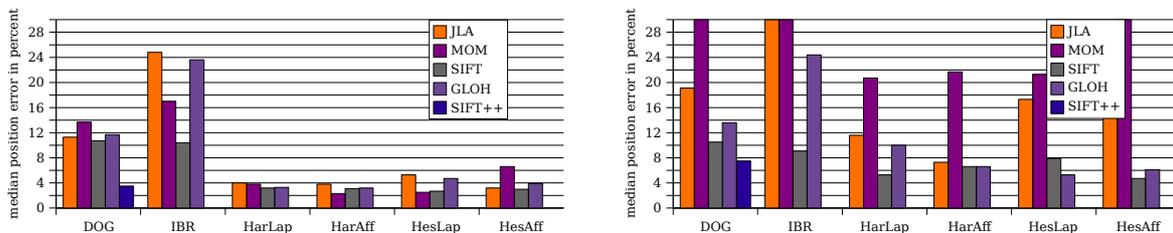


Figure 5: Multi camera calibration: median of median camera position errors in percent (truncated at 30) for all detectors and descriptors using nearest neighbor matching. Left: multi camera system, right: robot arm.

Harris and Hessian detectors show the best overall performance. The influence of the affine region extension varies. The comparatively bad results of the difference of Gaussian (DOG) detector might be implementation and parameter specific. The SIFT++ implementation shows much better results. IBR is generally not very reliable. As for the descriptor, SIFT and GLOH give the best results with no clear winner. Steerable filters (JLA) and invariant moments (MOM) can give similarly good results as SIFT and GLOH in some situations, but seem to be less robust.

## 5 Conclusions

We performed an experimental comparison of several interest point detectors, local descriptors and matching algorithms in the context of relative pose estimation and multi camera calibration. The results confirmed the good performance of the SIFT descriptor. Combined with the Harris/Hessian detectors, steerable filters and moment invariants could reach similar results, but were less reliable. The GLOH extension of SIFT did not show a pronounced improvement. The performance of the DOG detector depended on the implementation. The results of the SIFT++ version were close to the Harris/Hessian detectors, which gave the best results. As matching algorithm, two nearest neighbor was the best choice.

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